

ANURAG Engineering College

(An Autonomous Institution)

I B.Tech I Semester Supplementary Examinations, Jan/Feb-2024

MATHEMATICS – I**(COMMON TO ALL BRANCHES)****Time: 3 Hours****Max. Marks: 75****Section – A (Short Answer type questions)****(25 Marks)****Answer All Questions**

	Course Outcome	B.T Level	Marks
1. State Cauchy's mean value theorem.	CO1	L2	2M
2. Verify Lagrange's mean value theorem for $f(x) = \log_e x$ in $[1, e]$.	CO1	L2	3M
3. Define normal form of a matrix and give example.	CO2	L1	2M
4. Find the value of 'k' if the rank of the matrix A is 2	CO2	L1	3M
where $A = \begin{bmatrix} 1 & 2 & 7 \\ 2 & k & 7 \\ 3 & 6 & 10 \end{bmatrix}$.			
5. If $\lambda^3 + \lambda^2 - 21\lambda - 45 = 0$ is the characteristic equation of matrix A find $\det(A)$.	CO3	L2	2M
6. Let A be a square matrix of order 3 with Eigen values 2, 2 and 3 and A is diagonalizable then find rank of $(A-2I)$.	CO3	L2	3M
7. Form the differential equation by eliminating the arbitrary constant $y^2 = (x - c)^2$.	CO4	L2	2M
8. Define Orthogonal Trajectories in Cartesian co-ordinates	CO4	L1	3M
9. Find the general solution of $f(D)y=0$	CO5	L1	2M
10. Solve $(D^2 - 4D + 13)y = e^{2x}$.	CO5	L2	3M

Section B (Essay Questions)**Answer all questions, each question carries equal marks.****(5 X 10M = 50M)**

11. A) Prove that $\frac{\pi}{6} + \frac{1}{5\sqrt{3}} < \sin^{-1}\left(\frac{3}{5}\right) < \frac{\pi}{6} + \frac{1}{8}$ using suitable mean value theorem.

CO1 L3 10M

OR

B) Verify Rolle's theorem for the function $f(x) = \log\left\{\frac{x^2+ab}{x(a+b)}\right\}$ in $[a, b]$ where $a > 0, b > 0$.

CO1 L3 10M

12. A) Reduce the matrix $\begin{bmatrix} 10 & -2 & 3 & 0 \\ 2 & 10 & 2 & 4 \\ -1 & -2 & 10 & 1 \\ 2 & 3 & 4 & 9 \end{bmatrix}$ to echelon form and hence find its rank.

CO2 L3 10M

OR

B) Find the inverse of the matrix $A = \begin{bmatrix} -1 & -3 & 3 & -1 \\ 1 & 1 & -1 & 0 \\ 2 & -5 & 2 & -3 \\ -1 & 1 & 0 & 1 \end{bmatrix}$ using Gauss-Jordan method.

CO2 L3 10M

13. A) Find Eigen values and Eigen vectors of $\begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}$. CO3 L3 10M

OR

- B) State Cayley-Hamilton theorem and verify the Cayley-Hamilton for the matrix $A = \begin{bmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{bmatrix}$. CO3 L3 10M

14. A) Solve $(x^2 - y^2)dx = 2xy dy$. CO4 L3 10M

OR

- B) A body kept in air with temperature 25°C cool from 140°C to 80°C in 20 minutes. Find when the body cools down to 35°C . CO4 L3 10M

15. A) Solve $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 3y = e^{2x}$. CO5 L3 10M

OR

- B) A particle is executing simple harmonic motion of period T about a centre O and it passes through position P (OP=b) with velocity v in the direction OP. Show that the time that elapses before it returns to P $\frac{T}{\pi} \tan^{-1} \frac{vT}{2\pi b}$. CO5 L3 10M